

Self-Mixing Amplifier for CW Sensors

Master thesis presentation

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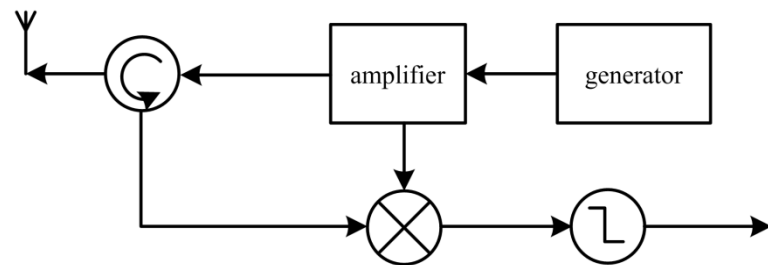
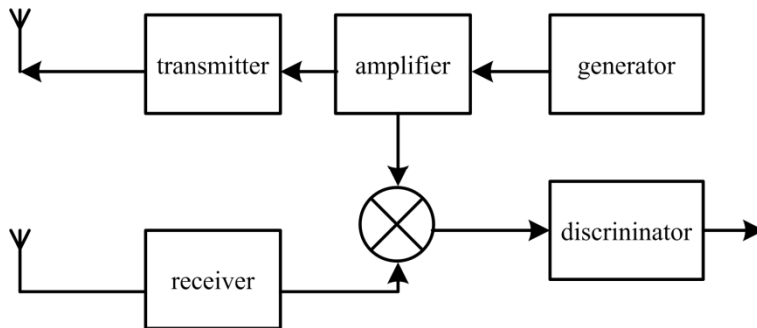
- Motivation
- 10 MHz Single Stage Amplifier Analysis
- Design and Measurement of 10 GHz Self-Mixing Amplifier
- Conclusion

Motivation

- Background
- Nonlinear Fundamentals
- Mixer Fundamentals

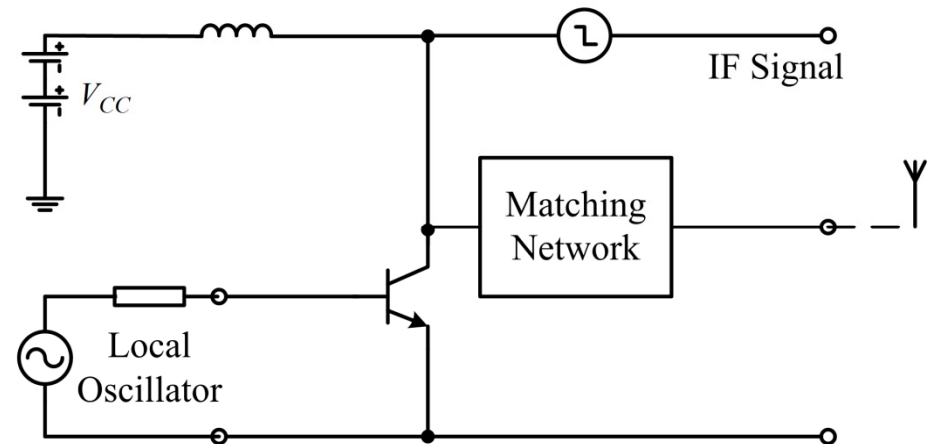
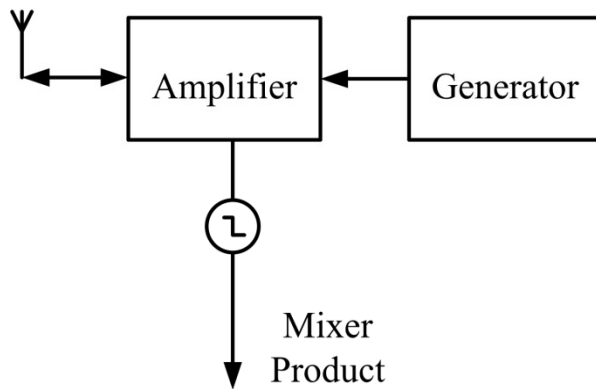
Motivation - Background

- CW Sensor
- Traditional transmitter and receiver designs



Motivation - Background

● New concept



Motivation – Nonlinear Fundamentals



● Nonlinear network analysis

$$v_{\text{out}} = a_0 + a_1 v_{\text{in}} + a_2 v_{\text{in}}^2 + a_3 v_{\text{in}}^3 + \dots$$

$$a_0 = v_{\text{out}}(0)$$

$$a_1 = \left. \frac{dv_{\text{out}}}{dv_{\text{in}}} \right|_{v_{\text{in}}=0} \quad a_2 = \left. \frac{d^2 v_{\text{out}}}{dv_{\text{in}}^2} \right|_{v_{\text{in}}=0} \quad a_3 = \left. \frac{d^3 v_{\text{out}}}{dv_{\text{in}}^3} \right|_{v_{\text{in}}=0}$$

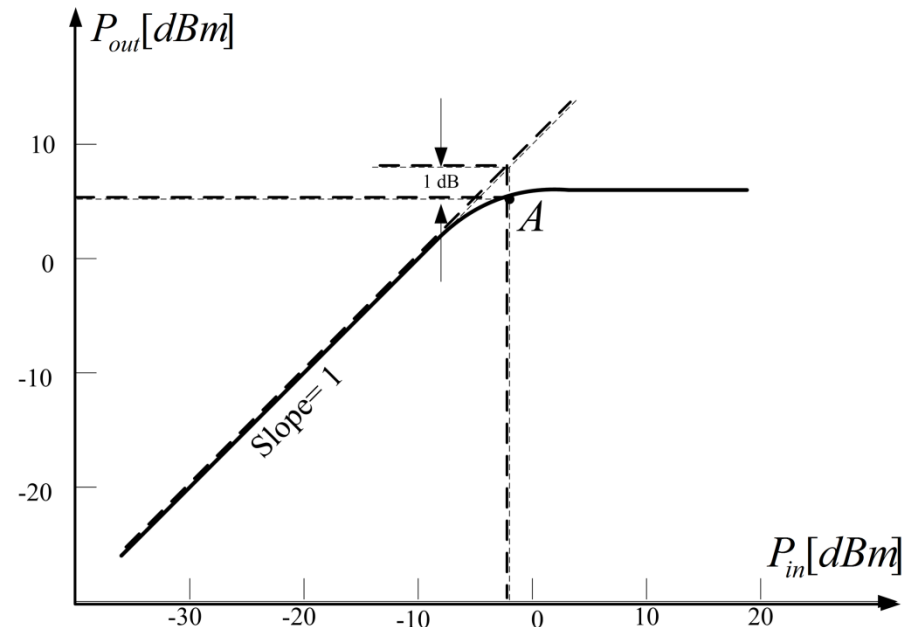
If $v_{\text{in}} = V_0 \cos \omega_0 t$, the output voltage is

$$v_{\text{out}} = (a_0 + \frac{1}{2} a_2 V_0^2) + (a_1 V_0 + \frac{3}{4} a_3 V_0^3) \cos \omega_0 t + \frac{1}{2} a_2 V_0^2 \cos 2\omega_0 t + \dots$$

Motivation – Nonlinear Fundamentals



- Voltage gain (retained to the third order) $G_v = a_1 + \frac{3}{4} a_3 V_0^2$
- 1 dB-Compression Point



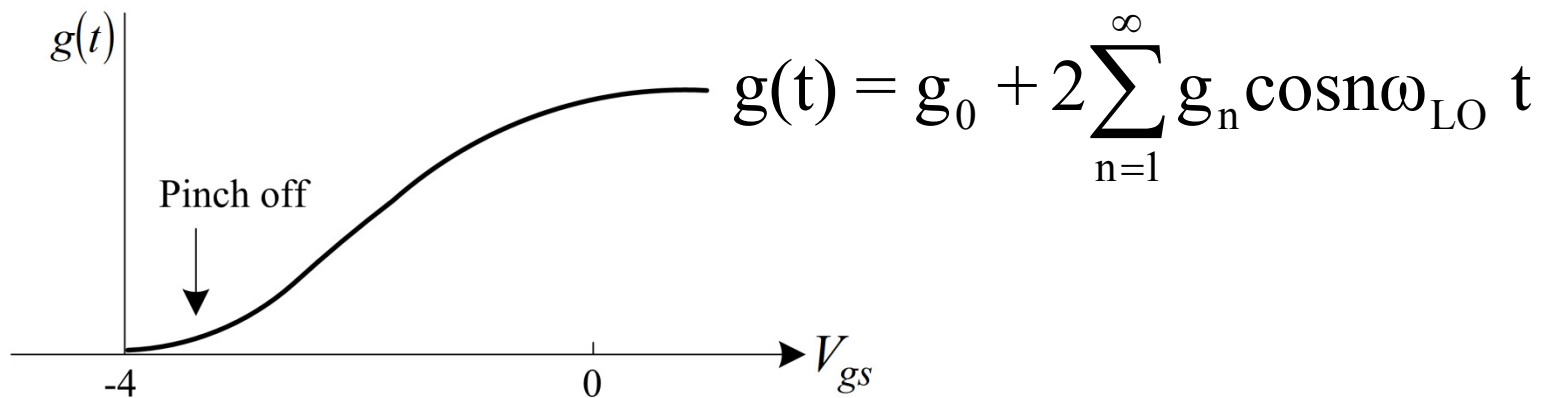
Motivation – Mixer Fundamentals



● Down conversion $f_{IF} = f_{RF} - f_{LO}$

● Conversion Loss $L_c = 10 \log \frac{P_{RF}}{P_{IF}} > 0 \text{ dB}$

● Variation of FET Output Conductance



Motivation – Mixer Fundamentals



● Drain current

$$\begin{aligned} i(t) &= g(t) v_{\text{RF}}(t) = V_{\text{RF}} \left[g_0 \cos \omega_{\text{RF}} t + 2 \sum_{n=1}^{\infty} g_n \cos n \omega_{\text{LO}} t \cos \omega_{\text{RF}} t \right] \\ &= V_{\text{RF}} \left[g_0 \cos \omega_{\text{RF}} t + 2 \sum_{n=1}^{\infty} g_n \left[\cos n(\omega_{\text{RF}} + n \omega_{\text{LO}}) t + \cos n(\omega_{\text{RF}} - n \omega_{\text{LO}}) t \right] \right] \end{aligned}$$

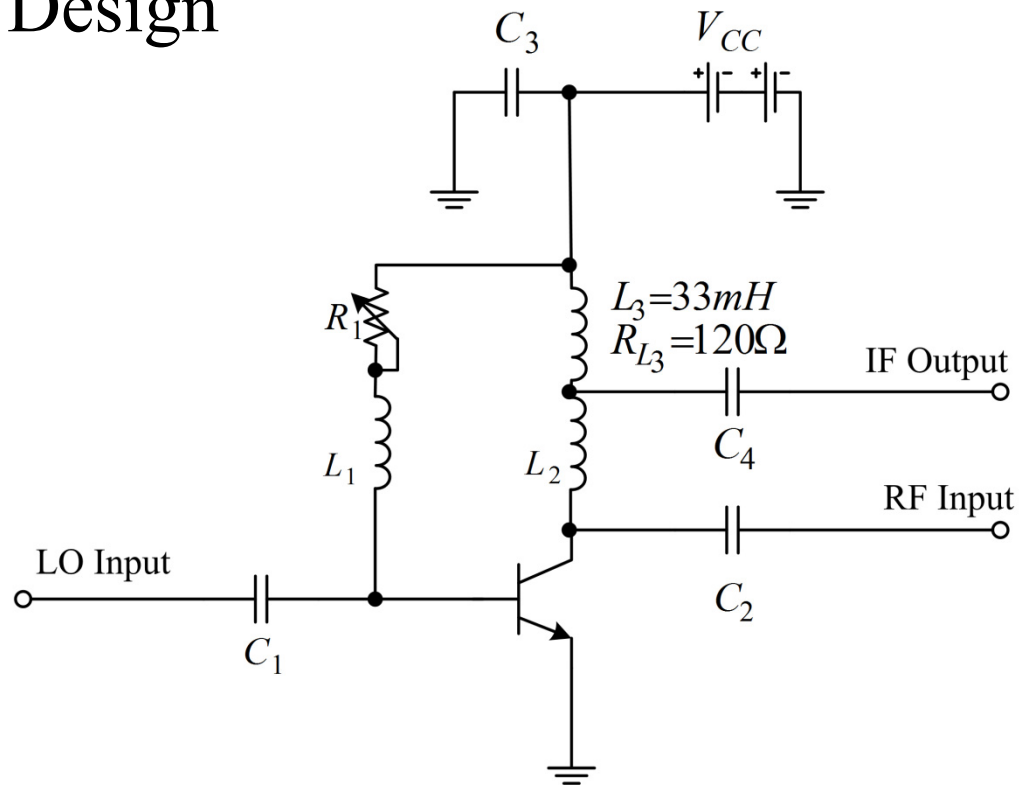
10 MHz Single Stage Amplifier Analysis

- Simulation

- Measurement

10 MHz Single Stage Amplifier Analysis – Simulation

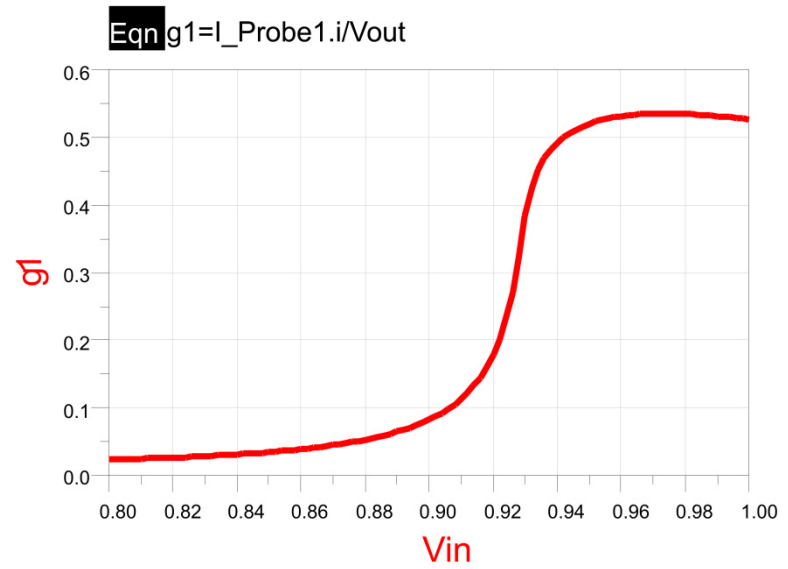
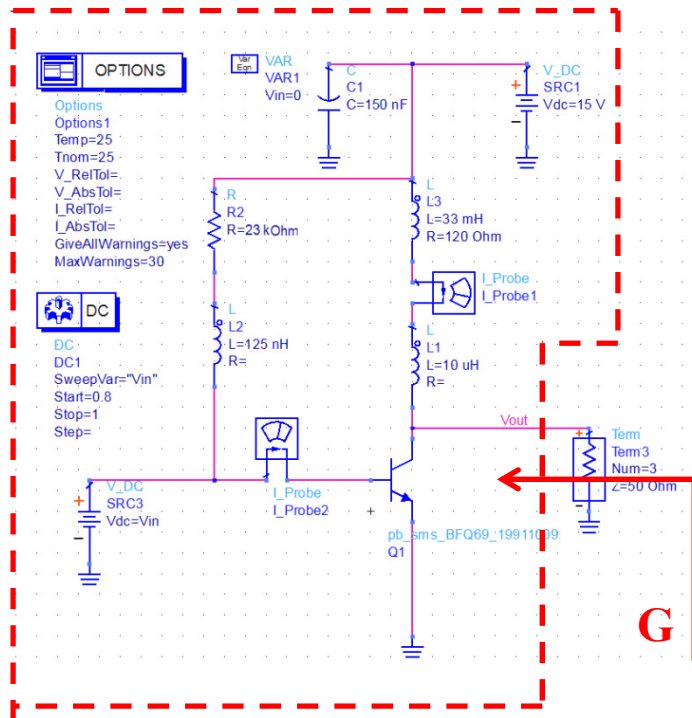
● Circuit Design



10 MHz Single Stage Amplifier Analysis – Simulation



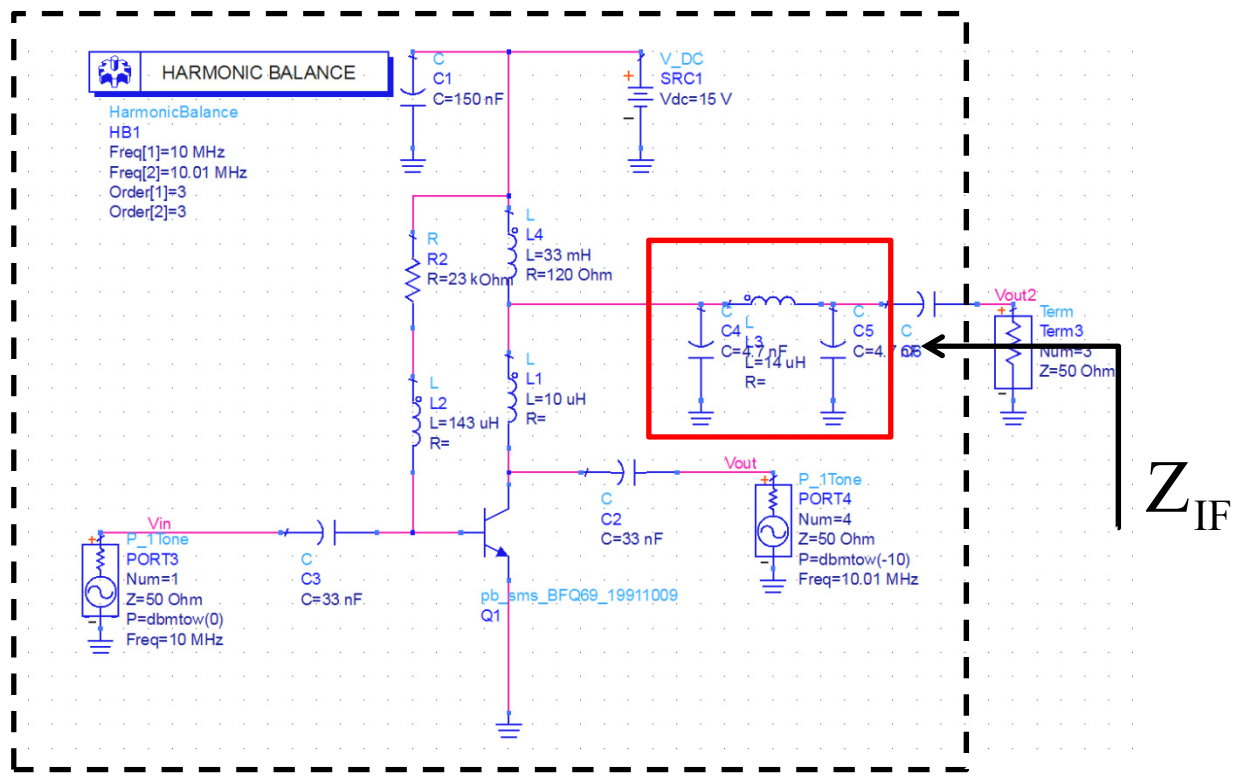
● Amplifier output Conductance



10 MHz Single Stage Amplifier Analysis – Simulation



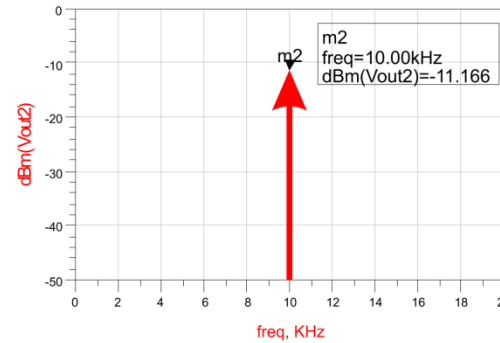
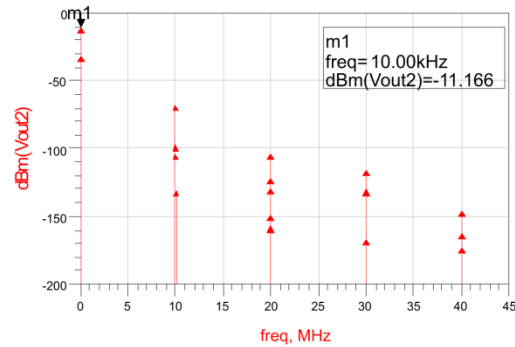
● Mixer Characteristics



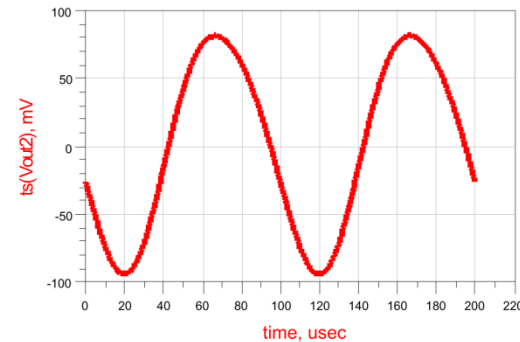
10 MHz Single Stage Amplifier Analysis – Simulation



● Mixer Characteristics

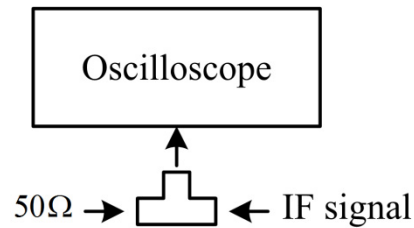
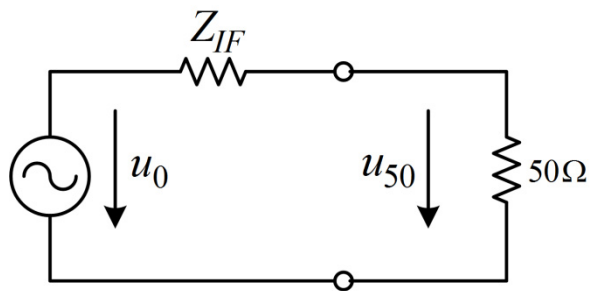


freq	Mix(1)	Mix(2)
0.0000 Hz	0	0
10.00 kHz	-1	1
20.00 kHz	-2	2
9.990 MHz	2	-1
10.00 MHz	1	0
10.01 MHz	0	1
10.02 MHz	-1	2
19.99 MHz	3	-1
20.00 MHz	2	0
20.01 MHz	1	1
20.02 MHz	0	2
20.03 MHz	-1	3
30.00 MHz	3	0
30.01 MHz	2	1
30.02 MHz	1	2
30.03 MHz	0	3
40.01 MHz	3	1
40.02 MHz	2	2
40.03 MHz	1	3



10 MHz Single Stage Amplifier Analysis – Measurement

- Methods of Measurement
 - Spectrum Analyzer
 - Oscilloscope



$$P_{\text{out}} [\text{dBm}] = 10 \log \frac{P_{\text{out}}}{1 \text{mW}}$$

$$P_{\text{out}} = \frac{u_{50\text{rms}}^2}{50 \Omega}$$

$$Z_{\text{IF}} = \frac{u_0}{u_{50}} 50 \Omega - 50 \Omega$$

10 MHz Single Stage Amplifier Analysis – Measurement

● Measurement with a Spectrum Analyzer

Unit	LO, RF and IF signal [dBm]						Conversion Loss [dB]	
RF signal	LO signal							
	0		5		10		15	
	IF signal	Conversion Loss	IF signal	Conversion Loss	IF signal	Conversion Loss	IF signal	Conversion Loss
-10	-34.2	24.2	-26.4	16.4	-23.2	13.2	-21.0	11.0
-15	-39.4	24.4	-32.2	17.2	-28.3	13.3	-26.3	11.3
-20	-44.9	24.9	-37.3	17.3	-33.3	13.3	-31.3	11.3
-25	-47.8	22.8	-41.3	16.3	-38.2	13.2	-36.3	11.3
-30	-52.3	22.3	-46.7	16.7	-43.3	13.3	-41.5	11.5
-40	-		-		-53.5	13.5	-51.5	11.5

10 MHz Single Stage Amplifier Analysis – Measurement

● Measurement with an Oscilloscope

LO Signal [dBm]	RF Signal [dBm]			
	-10			
	Open[mV]	50Ω [mV]	Impedance[Ω]	Output Power[dBm]
0	9.84	4.52	58.85	-33.88
5	22.77	10.90	54.45	-26.24
10	31.91	15.51	52.87	-23.18
15	40.98	19.95	52.63	-20.10

10 MHz Single Stage

Amplifier Analysis – Measurement

- Measurement of the Amplifier Output Conductance (RF Input Conductance)

Input Power[dBm]	v_in[mV]	v_out[mV]	v_out_50Ω [mV]	Z[Ω]	G[mS]
-30	15	332	147	62.98	15.9
-25	26	580	258	62.33	16.0
-20	49	990	453	59.38	16.8
-15	86	1.54 *10 ³	707	59	16.9
-10	155	2.03 *10 ³	1.00 *10 ³	51.5	19.4
-5	271	2.70 *10 ³	1.26 *10 ³	57.14	17.5
-3	336	2.77 *10 ³	1.28 *10 ³	58.20	17.2

Design and Measurement of 10 GHz Self-Mixing Amplifier

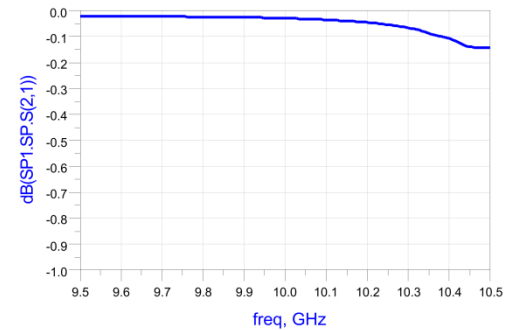
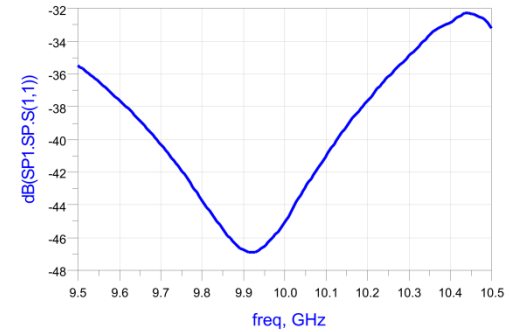
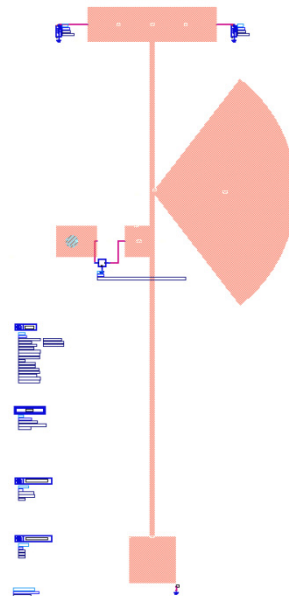
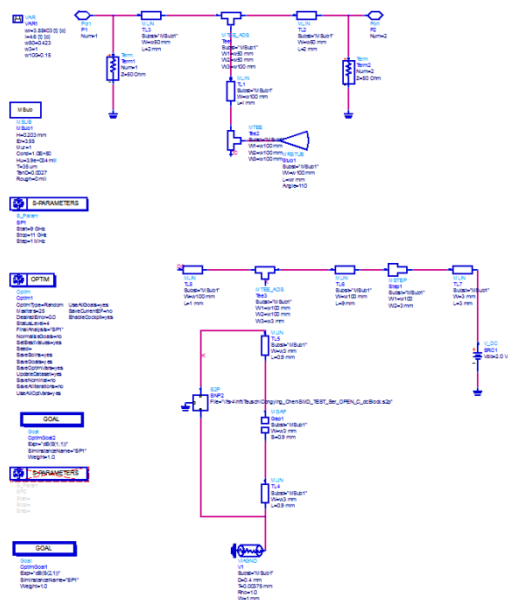
- Design and Simulation

- Measurement

Design and Measurement of 10 GHz Self-Mixing Amplifier

– Design and Simulation

- Transistor Selection & Operating Point
- Bias network Design



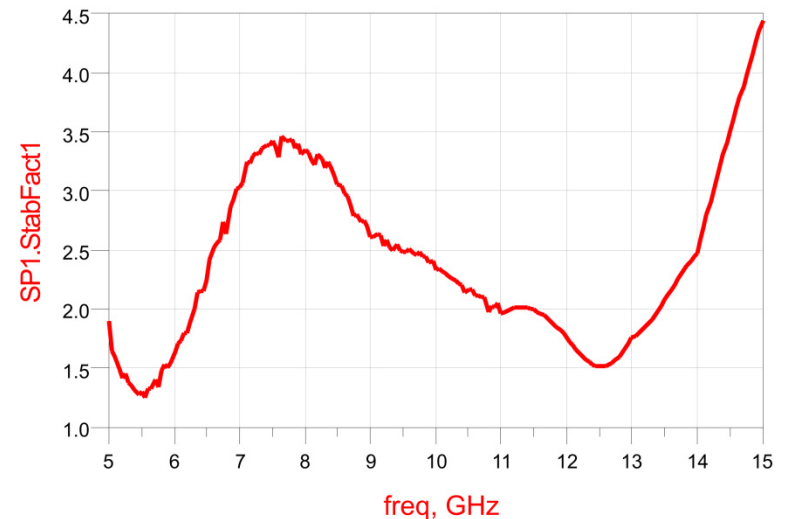
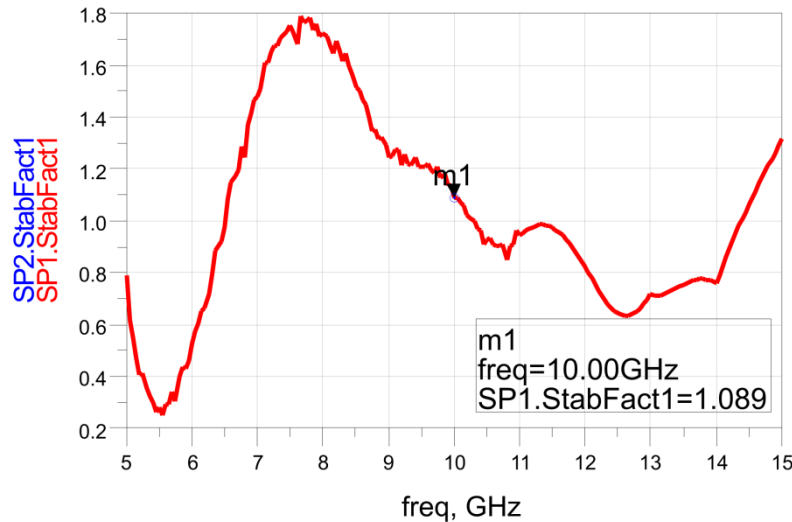
Design and Measurement of 10 GHz Self-Mixing Amplifier

– Design and Simulation

● Stability Analysis

$$K = \frac{(1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2)}{2 |S_{12} S_{21}|} > 1$$

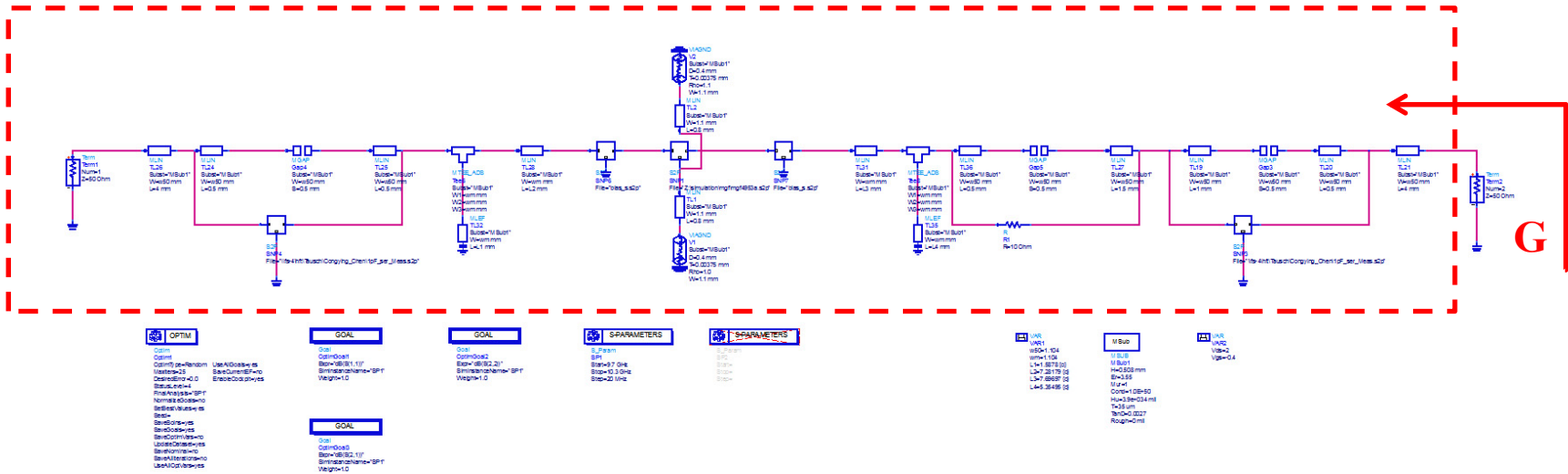
$$|\Delta| = |S_{11} S_{22} - S_{12} S_{21}| < 1$$



Design and Measurement of 10 GHz Self-Mixing Amplifier

– Design and Simulation

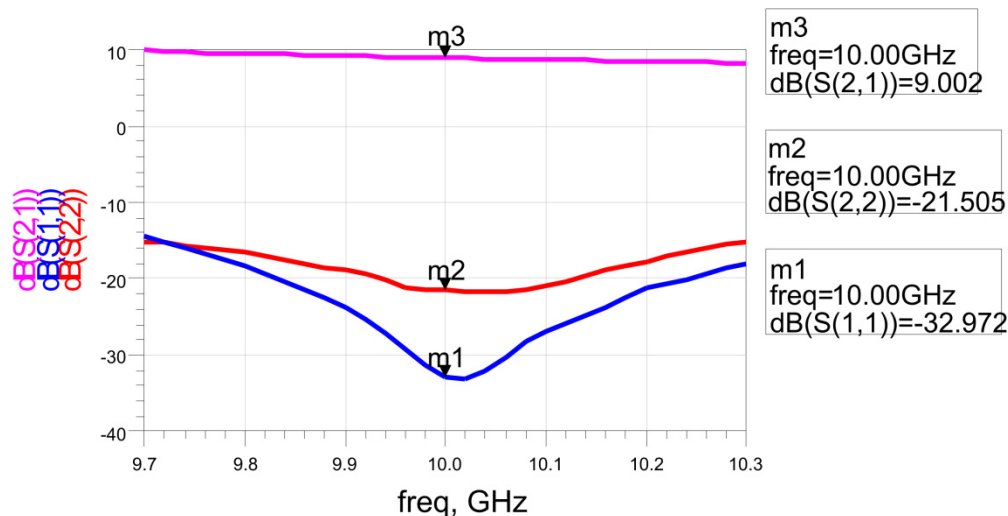
● Input and output matching and Overall Amplifier



Design and Measurement of 10 GHz Self-Mixing Amplifier

– Design and Simulation

- Input and output matching and Overall Amplifier

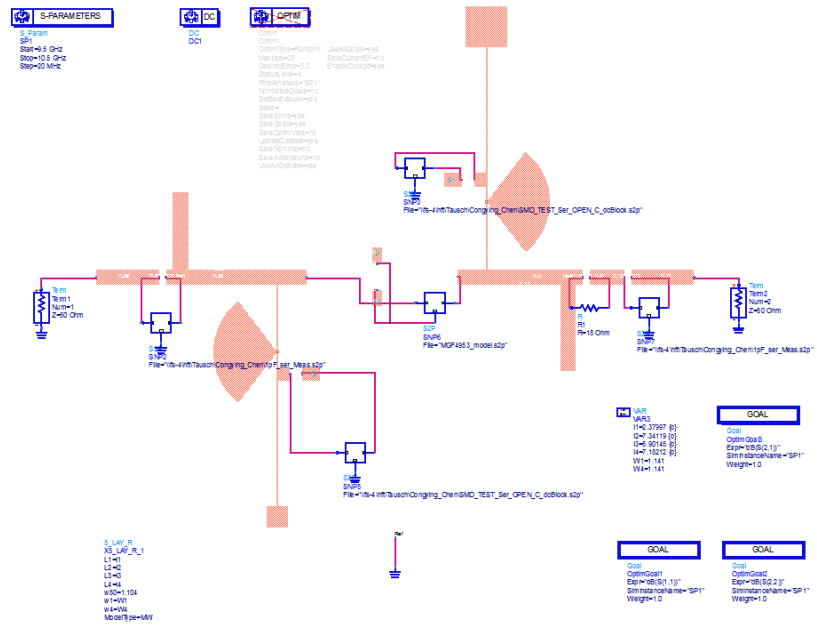


Design and Measurement of 10 GHz Self-Mixing Amplifier

– Design and Simulation



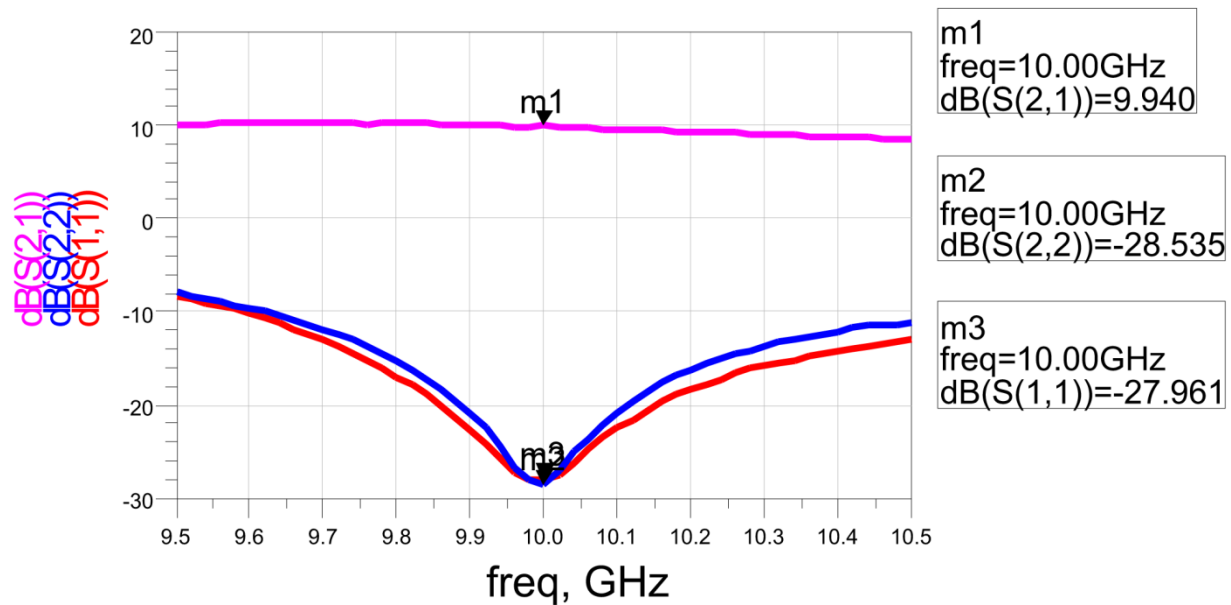
- Input and output matching and Overall Amplifier



Design and Measurement of 10 GHz Self-Mixing Amplifier

- Design and Simulation

- Input and output matching and Overall Amplifier

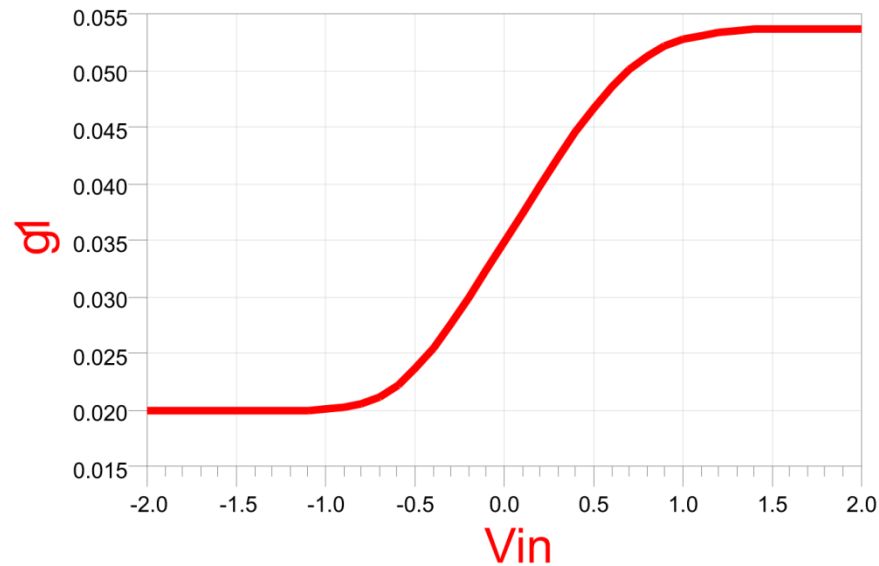


Design and Measurement of 10 GHz Self-Mixing Amplifier

– Design and Simulation

● RF Input Conductance

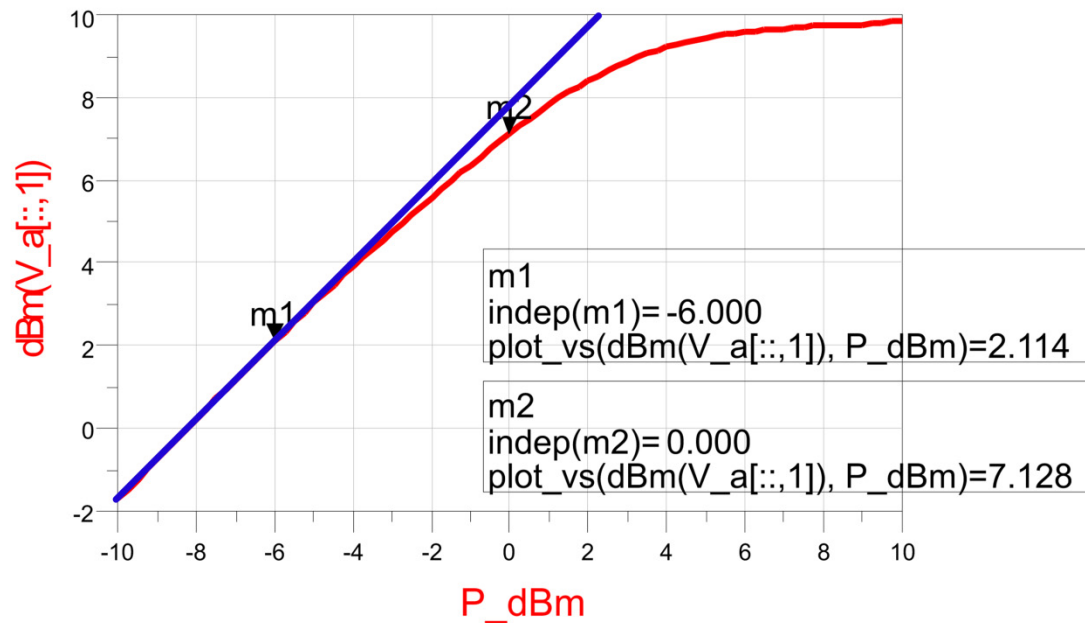
Eqn $g_1 = I_{\text{Probe1.i}} / V_{\text{out}}$



Design and Measurement of 10 GHz Self-Mixing Amplifier

- Design and Simulation

● 1 dB Compression Point

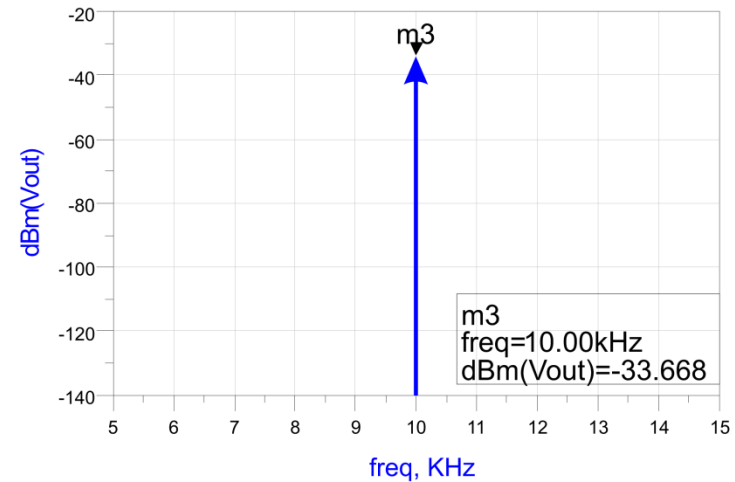
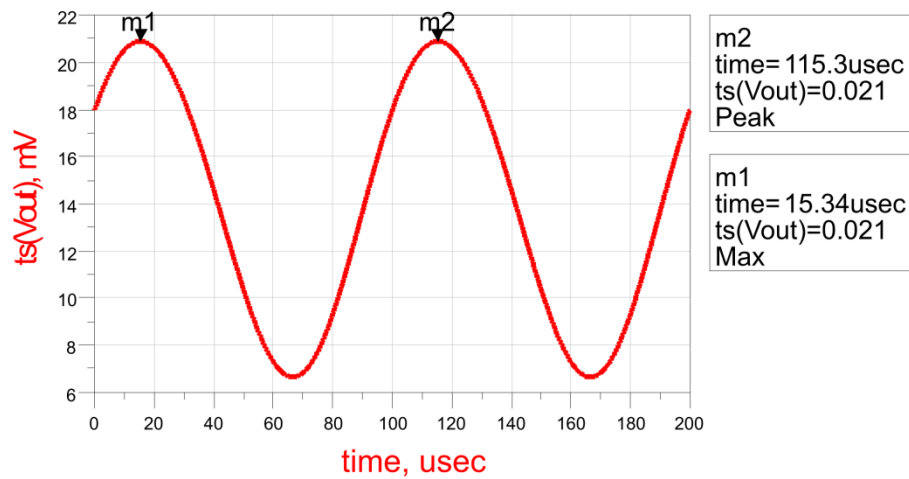


Design and Measurement of 10 GHz Self-Mixing Amplifier

- Design and Simulation



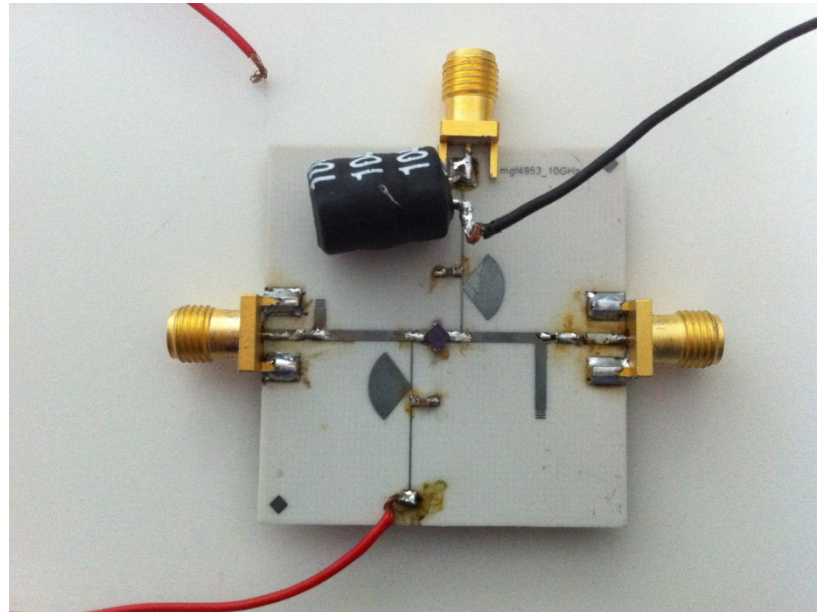
● IF Signal



Design and Measurement of 10 GHz Self-Mixing Amplifier

– Measurement

● Implementation

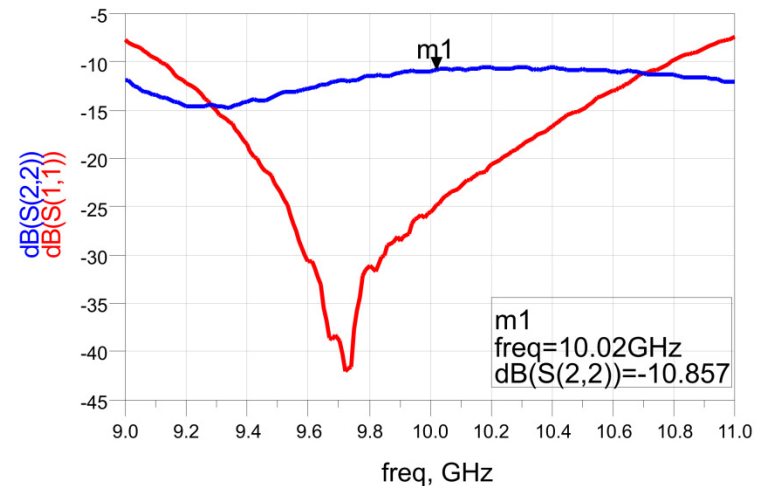
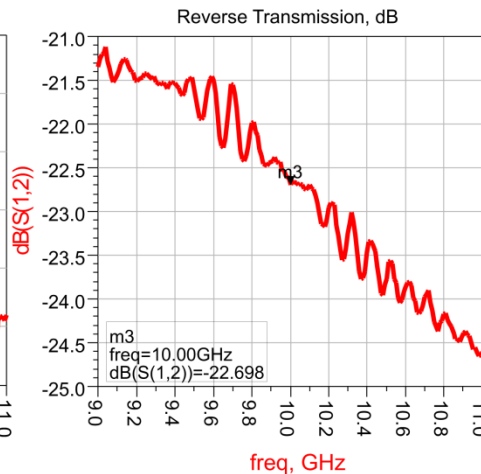
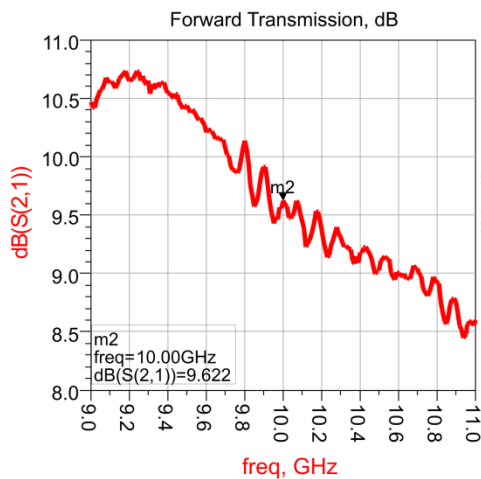


Design and Measurement of 10 GHz Self-Mixing Amplifier



– Measurement

● Measurement of the S Parameters



Design and Measurement of 10 GHz Self-Mixing Amplifier

– Measurement

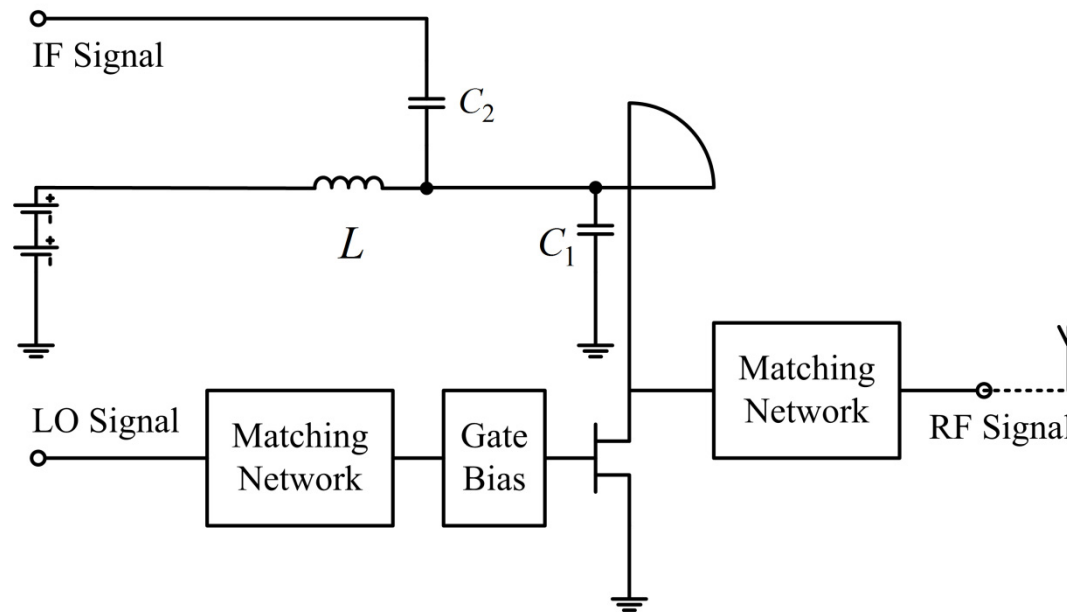
● Measurement of 1 dBm-Compression Point

Input Power[dBm]	-10	-8	-6	-4	-2	0	2
Output Power[dBm]	-0.49	1.51	3.51	5.40	7.17	8.50	9.50

Design and Measurement of 10 GHz Self-Mixing Amplifier

– Measurement

● Measurement of the Mixer Conversion Loss



$$L = 100 \text{ mH}$$

$$C_2 = 1.5 \mu\text{F}$$

$$C_2 > \frac{1}{2\pi f_{\text{IF}}}$$

Design and Measurement of 10 GHz Self-Mixing Amplifier

– Measurement

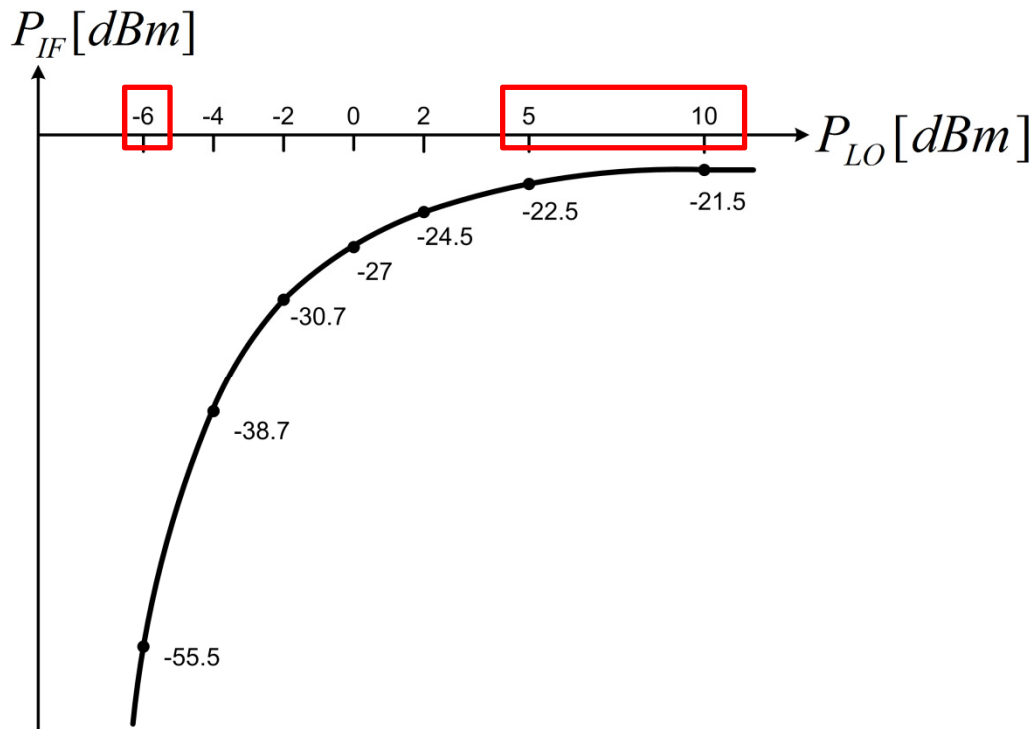
● Mixer Products (Spectrum Analyzer)

RF Signal [dBm]	LO Signal[dBm]					
	-2		0		2	
	IF Signal [dBm]	Conversion Loss[dB]	IF Signal [dBm]	Conversion Loss[dB]	IF Signal [dBm]	Conversion Loss[dB]
-10	-30.79	20.79	-27.00	17.00	-24.50	14.50
-15	-36.99	21.99	-32.10	17.10	-29.97	14.97
-20	-40.51	20.51	-38.52	18.52	-35.10	15.10
-25	-45.70	20.70	-43.00	18.00	-39.03	14.03

Design and Measurement of 10 GHz Self-Mixing Amplifier

– Measurement

● Mixer Products (Spectrum Analyzer)



$$P_{RF} = -10\text{dBm}$$

Design and Measurement of 10 GHz Self-Mixing Amplifier

– Measurement

- Mixer Products (Oscilloscope) without C_2

LO Signal [dBm]	RF Signal [dBm]			
	-10			
	Open[mV]	50Ω[mV]	Impedance[Ω]	Output Power[dBm]
-2	68	40	35.00	-23.98
0	98	60	31.66	-20.46
2	104	64	31.25	-19.89

Design and Measurement of 10 GHz Self-Mixing Amplifier

– Measurement

- Mixer Products (Oscilloscope) with C_2

LO Signal [dBm]	RF Signal [dBm]			
	-10			
	Open[mV]	50Ω [mV]	Impedance[Ω]	Output Power[dBm]
-2	35	20	37.50	-30.00
0	52	31	33.87	-26.19
2	70	42	33.33	-23.55

Design and Measurement of 10 GHz Self-Mixing Amplifier

– Measurement

- Calculation of Impedance in Imagine Part

Impedance[Ω] Measured without C_2	Impedance[Ω] Measured with C_2	Impedance[Ω] of C_2
35.00	37.50	13.46
31.66	33.87	12.03
31.25	33.33	11.58

Design and Measurement of 10 GHz Self-Mixing Amplifier

– Measurement

- Conversion Loss

LO Signal[dBm]	Conversion Loss[dB]
-2	13.98
0	10.46
2	9.89

Conclusion

- Larger LO Signal → Larger Output Signal
Lower Output Impedance
- The LO Signal depends on 1 dB-compression point
- Feasibility of Self-Mixing Amplifier

Thank You for Your Attention